MASTER OF SCIENCE IN MATHEMATICS

Program Director
Dr. G. Jay Kerns
620 Lincoln Building
(330) 941-3310
gkerns@ysu.edu

Program Description
The Department of Mathematics and Statistics offers the M.S. degree in mathematics both traditionally and online. Options for this degree include:

- predoctoral studies,
- applied mathematics,
- computer science,
- secondary mathematics,
- statistics, and
- actuarial science.

Graduate faculty members have a broad range of research interests in both pure and applied areas. The curriculum stresses theoretical as well as computational mathematics and is flexible enough to key a student’s program to individual interests and abilities. Receiving a well-rounded education in mathematics, graduates can pursue a Ph.D., secure a position in government or industry, or further a teaching career.

The Department of Mathematics and Statistics also offers a Graduate Certificate in Mathematics and a Graduate Certificate in Data Analytics

Admission Requirements
In addition to the minimum College of Graduate Studies admission requirements, students must also have the following:

<table>
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<tr>
<th>COURSE</th>
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<tbody>
<tr>
<td>A cumulative undergraduate cumulative grade point average of at least 3.0 (on a 4.0 scale) in all undergraduate mathematics and statistics courses.</td>
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<tr>
<td>A completed sequence in standard calculus comparable to:</td>
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<tr>
<td>MATH 1571</td>
<td>Calculus 1</td>
<td>4</td>
</tr>
<tr>
<td>MATH 1572</td>
<td>Calculus 2</td>
<td>4</td>
</tr>
<tr>
<td>MATH 2673</td>
<td>Calculus 3</td>
<td>4</td>
</tr>
<tr>
<td>Previous courses in discrete structures and linear algebra comparable to:</td>
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<td></td>
</tr>
<tr>
<td>MATH 3715</td>
<td>Discrete Mathematics</td>
<td>3</td>
</tr>
<tr>
<td>MATH 3720</td>
<td>Linear Algebra and Matrix Theory</td>
<td>3</td>
</tr>
<tr>
<td>Previous courses in abstract algebra and real analysis comparable to:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>MATH 5821</td>
<td>Topics in Abstract Algebra</td>
<td>4</td>
</tr>
<tr>
<td>MATH 5851</td>
<td>Topics in Analysis</td>
<td>4</td>
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</tbody>
</table>

Students not satisfying all of the above may be admitted with provisional status subject to the approval of the graduate program director and the graduate dean.

Graduate Faculty
Alexis Byers, Ph.D., Assistant Professor
Graph Theory

Guang-Hwa (Andy) Chang, Ph.D., Professor
Biostatistics

Neil Flowers, Ph.D., Assistant Professor
Solvable groups; classification problems in group theory

Richard G. Goldthwait, Ph.D., Assistant Professor
Math education

Jozsi Z. Jalics, Ph.D., Professor
Computational neuroscience; mathematical biology; dynamical systems; partial differential equations

G. Jay Kerns, Ph.D., Professor
Signed measures; infinite divisibility; exchangeability in probability and statistics; applications of stochastic processes

Lucy Xiaojing Kerns, Ph.D., Associate Professor
Simultaneous confidence bands; minimum effective doses; benchmark dose methodology

Thomas L. Madsen, Ph.D., Associate Professor
Abstract algebra; group theory; representation theory

Nguyet Thi Nguyen, Ph.D., Associate Professor
Financial models; Monte Carlo simulation; actuarial science

Anita C. O’Melian, Ph.D., Professor
Graph theory; combinatorics; early childhood mathematics education

Alicia Prieto Langarica, Ph.D., Professor
Mathematical biology; agent-based modeling

Stephen Rodabaugh, Ph.D., Professor
Foundations of topology and fuzzy logic: point-set, lattice-theoretic, and categorical methods

Thomas Smotzer, Ph.D., Professor
Real analysis; measure theory; operator theory

Jamal K. Tartir, Ph.D., Professor
Set-theoretic topology

Padraic (“Paddy”) W. Taylor, Ph.D., Associate Professor
Multipoint Boundary Value Problems

Thomas P. Wakefield, Ph.D., Professor, Chair
Character theory; actuarial science

Eric J. Wingler, Ph.D., Professor
Real analysis; complex analysis; operator theory

- A minimum of 30 semester hours of credit excluding MATH 5821 Topics in Abstract Algebra and MATH 5851 Topics in Analysis
- A cumulative grade point average of at least 3.0
- Students entering without a prior course in abstract algebra must include MATH 5821 Topics in Abstract Algebra in their program, to be taken in the earliest available semester, and students entering without a prior course in theoretical analysis must include MATH 5851 Topics in Analysis in their program, to be taken in the earliest available semester. These courses are not included in the 30-semester-hour minimum requirement.
- The student’s combined undergraduate and graduate programs must include a mathematics core comprising the following courses or their equivalent:

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<tr>
<td>MATH 5821</td>
<td>Topics in Abstract Algebra (taken in the earliest available semester)</td>
<td>4</td>
</tr>
<tr>
<td>MATH 5851</td>
<td>Topics in Analysis (taken in the earliest available semester)</td>
<td>4</td>
</tr>
<tr>
<td>MATH 5825</td>
<td>Advanced Linear Algebra</td>
<td>3</td>
</tr>
<tr>
<td>MATH 5852</td>
<td>Real Analysis 2</td>
<td>3</td>
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Choose one of the following:
elective courses based upon the recommendations below. Students with particular interests or career goals are advised to choose from the following list. The sequences offered depend upon student interest.

### Course Sequences for Depth

#### Students satisfy the depth requirement for the degree by choosing a sequence from the following list. The sequences offered depend upon student interest.

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<tr>
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<tr>
<td>MATH 6922</td>
<td>Advanced Topics in Group and Ring Theory</td>
<td>3</td>
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<tr>
<td>MATH 6923</td>
<td>Advanced Topics in Field Theory</td>
<td>3</td>
</tr>
<tr>
<td>MATH 6975</td>
<td>Complex Analysis 1</td>
<td>3</td>
</tr>
<tr>
<td>MATH 5852</td>
<td>Real Analysis 2</td>
<td>3</td>
</tr>
<tr>
<td>MATH 6980</td>
<td>Topology 1</td>
<td>3</td>
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<tr>
<td>STAT 6940</td>
<td>Advanced Data Analysis</td>
<td>3</td>
</tr>
<tr>
<td>MATH 6955</td>
<td>Advanced Differential Equations</td>
<td>3</td>
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<tr>
<td>STAT 6944</td>
<td>Mathematical Statistics 1</td>
<td>3</td>
</tr>
<tr>
<td>MATH 5861</td>
<td>Numerical Analysis 2</td>
<td>3</td>
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<tr>
<td>MATH 5845</td>
<td>Operations Research</td>
<td>3</td>
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#### Statistics

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<tr>
<td>STAT 6940</td>
<td>Advanced Data Analysis</td>
<td>3</td>
</tr>
<tr>
<td>STAT 6948</td>
<td>Linear Models</td>
<td>3</td>
</tr>
<tr>
<td>STAT 6943</td>
<td>Mathematical Statistics 1</td>
<td>3</td>
</tr>
<tr>
<td>STAT 6944</td>
<td>Mathematical Statistics 2</td>
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#### Actuarial Science

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<tr>
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<tbody>
<tr>
<td>STAT 5802</td>
<td>Theory of Interest</td>
<td>3</td>
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<tr>
<td>STAT 6943</td>
<td>Mathematical Statistics 1</td>
<td>3</td>
</tr>
<tr>
<td>STAT 6944</td>
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</tbody>
</table>

#### Applied Mathematics

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<td>3</td>
</tr>
<tr>
<td>MATH 6955</td>
<td>Advanced Differential Equations</td>
<td>3</td>
</tr>
<tr>
<td>STAT 6943</td>
<td>Mathematical Statistics 1</td>
<td>3</td>
</tr>
<tr>
<td>MATH 5860</td>
<td>Numerical Analysis 1</td>
<td>3</td>
</tr>
<tr>
<td>MATH 5861</td>
<td>Numerical Analysis 2</td>
<td>3</td>
</tr>
<tr>
<td>MATH 5845</td>
<td>Operations Research</td>
<td>3</td>
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#### Secondary/Community College Mathematics

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<tr>
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<tbody>
<tr>
<td>STAT 6943</td>
<td>Mathematical Statistics 1</td>
<td>3</td>
</tr>
<tr>
<td>STAT 6940</td>
<td>Advanced Data Analysis</td>
<td>3</td>
</tr>
<tr>
<td>MATH 6915</td>
<td>Mathematical Foundations</td>
<td>3</td>
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<tr>
<td>MATH 6922</td>
<td>Advanced Topics in Group and Ring Theory</td>
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<td>MATH 6923</td>
<td>Advanced Topics in Field Theory</td>
<td>3</td>
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<tr>
<td>MATH 6975</td>
<td>Complex Analysis 1</td>
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</tr>
<tr>
<td>MATH 6980</td>
<td>Topology 1</td>
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Those students seeking certification should consult an advisor in the Department of Teacher Education.

#### Computer Science

Students in coursework in computer science in addition to mathematics should plan their graduate program in consultation with advisors in both the Department of Mathematics and Statistics and the School of Computer Science, Information and Engineering Technology.

#### Accelerated MS Mathematics

Undergraduate students can apply for admission into the accelerated program for the MS in Mathematics after completing 78 semester hours with a GPA of 3.3 or higher. After being admitted into the program, students can

• Satisfactory performance on written and oral examinations. The subject matter for these examinations must be approved by the Graduate Executive Committee. Additionally, the following distribution requirements apply:
  - Written exams in MATH 5852, Math 5825 and the first course in the student's chosen course sequence
  - Oral exam on thesis, or oral exam on a project and two courses
  - At least half of the hours of the courses examined must be at the 6900 level

• At least 15 hours of the student's approved program must be at the 6900 level. In addition to completing the courses which make up the mathematics core, students must complete at least one course sequence for depth and at least fifteen additional hours of elective courses to satisfy the breadth requirement for the degree. The course groupings are described below.

• MATH 6999 Thesis is highly recommended

• Before completing 12 semester hours, the student must submit the entire degree program for approval and evaluation by the Graduate Executive Committee in the Department of Mathematics and Statistics. Subsequent revisions to this program must be approved by the Graduate Executive Committee. An abstract of a proposed thesis must be submitted for approval prior to registering for the course.

• Students must participate in an exit interview during the semester in which they plan on graduating. The exit interview will be conducted with one or more members of the Graduate Executive Committee and must be scheduled by the student prior to the thesis or project presentation.
Learning Outcomes
Students will develop and demonstrate the ability to reason mathematically by constructing mathematical proofs and recognizing and analyzing accurate numerical data in appropriate core courses. Students will learn that truth in mathematics is verified by careful argument, and will demonstrate the ability to make conjectures and form hypotheses, test the accuracy of their work, and effectively solve problems.

Students will learn to identify fundamental concepts of mathematics as applied to science and other areas of mathematics, and to interconnect the roles of pure and applied mathematics.

Students will demonstrate that they can communicate mathematical ideas effectively, both orally and in writing, by completing a graduate project or thesis involving an investigative mathematical project, together with oral and written examinations.

Students in cooperative doctoral programs will demonstrate their ability to create significant, original mathematics.

Graduate Courses
MATH 5821 Topics in Abstract Algebra 4 s.h.
A course in abstract algebra aimed at developing a broad understanding of the subject. Credit will not be given for both MATH 3721 and MATH 5821.
Prereq.: MATH 3715 and MATH 3720.

MATH 5825 Advanced Linear Algebra 3 s.h.
A study of abstract vector spaces, linear transformations, duality, canonical forms, the spectral theorem, and inner product spaces.
Prereq.: MATH 3721.

MATH 5828 Number Theory 3 s.h.
A study of congruences, Diophantine equations, quadratic residues, special number theory functions, and selected applications.
Prereq.: MATH 3721.

MATH 5835 Introduction to Combinatorics and Graph Theory 3 s.h.
The pigeonhole principle, permutations, combinations, the binomial theorem; the inclusion-exclusion principle; recurrence relations; graphs and digraphs, paths and cycles, trees, bipartite graphs and matchings.
Prereq.: C or better in either MATH 3715 or CSCI 3710 and C or better in MATH 3720.

MATH 5845 Operations Research 3 s.h.
An introduction to operations research with emphasis on mathematical methods. Topics may include: linear programming, sensitivity analysis, duality theory, transportation problems, assignment problems, transshipment problems, and network problems.
Prereq.: MATH 3715 and MATH 3720.

MATH 5851 Topics in Analysis 4 s.h.
A course in analysis aimed at developing a broad understanding of the subject. Credit will not be given for both MATH 3751 and MATH 5851.
Prereq.: MATH 2673 or MATH 2686H and MATH 3720 and MATH 3715.

MATH 5852 Real Analysis 2 3 s.h.
Uniform convergence of sequences of functions and some consequences; functions on n-space: derivatives in vector spaces, mean value theorem, Taylor’s formula, inverse mapping theorem, implicit mapping theorem.
Prereq.: MATH 3720 and MATH 3751 or equivalent.

MATH 5860 Numerical Analysis 1 3 s.h.
The theory and techniques of numerical computation. The solution of a single equation, interpolation methods, numerical differentiation and integration, direct methods for solving linear systems.
Prereq.: MATH 3720 and CSIS 2610 and MATH 2673, 2673H, or 2686H.

MATH 5861 Numerical Analysis 2 3 s.h.
Numerical methods of initial-value problems, eigenvalue problems, iterative methods for linear and nonlinear systems of equations, and methods involving least squares, orthogonal polynomials, and fast Fourier transforms.
Prereq.: MATH 5860 or equivalent.

MATH 5895 Selected Topics in Mathematics 2-3 s.h.
The study of a standard mathematical topic in depth or the development of a special area of mathematics. May be repeated twice.
Prereq.: 24 s.h. of mathematics applicable to the mathematics major including either MATH 3721 or MATH 3751.

MATH 6901 Mathematics Workshop 1-6 s.h.
Intensive study and activity in a topic related to mathematics, its applications, or the teaching of mathematics. May be repeated. Grading is S/U.
Prereq.: Permission of graduate coordinator.

MATH 6905 College Teaching of Mathematics 1 s.h.
Intensive preparation for teaching lower-level mathematics courses, featuring formal instruction and orientation on teaching issues, evaluated presentations, mentored classroom instruction, and weekly teaching seminars. Topics include course design, policies, syllabi, grading; classroom teaching problems; orientation in Mathematics Assistance Center, specific lower-level mathematics courses, online tutorial services. Required of graduate assistants in the Department of Mathematics and Statistics and to be taken each semester the student is a graduate assistant. Grading is S/U. Does not count toward credit in the program.

MATH 6910 Advanced Engineering Mathematics 1 3 s.h.
Theory and solution techniques used in engineering applications. Topics include brief review of ordinary differential equations and linear algebra; vector calculus, integral theorems, complex analysis, series, residue theory, potential theory, special functions, integral transforms, partial differential equations and applications in mathematical modeling.
Prereq.: MATH 3705.

MATH 6911 Advanced Engineering Mathematics 2 3 s.h.
Theory and solution techniques used in engineering applications. Topics include brief review of ordinary differential equations and linear algebra; vector calculus, integral theorems, complex analysis, series, residue theory, potential theory, special functions, integral transforms, partial differential equations and applications in mathematical modeling.
Prereq.: MATH 6910.

MATH 6915 Mathematical Foundations 3 s.h.
Order-theoretic and monadic foundations of mathematics: ordered structures; topologies; powerset operators of a function; applications to continuity, compactness, algebra, logic, and calculus.
Prereq.: MATH 3721 Abstract Algebra I and MATH 3751 Real Analysis I, or permission of graduate coordinator.

MATH 6922 Advanced Topics in Group and Ring Theory 3 s.h.
A continuation of MATH 5821 with special emphasis on groups acting on sets, Sylow’s Theorem and its applications, ring homomorphisms, ideals, and polynomial rings. Credit will not be given for MATH 4822 and MATH 6922.
Prereq.: MATH 3721 or MATH 5821.

MATH 6923 Advanced Topics in Field Theory 3 s.h.
This course introduces the major results in advanced field theory. These results include splitting fields, algebraic extensions, finite extensions, cyclotomic polynomials, and finite fields. Credit will not be given for MATH 4823 and MATH 6923.
Prereq.: MATH 4822 or MATH 6922.

MATH 6924 Galois Theory 3 s.h.
An introduction to Galois Theory with special emphasis on the Galois group, the Fundamental Theorem of Galois Theory, and radical extensions.
Prereq.: MATH 4823 or MATH 6923.
MATH 6936  Advanced Topics and Research in Graph Theory  3 s.h.
This is a research-based course in graph theory that builds upon knowledge
learned in MATH 5835. The research process of a mathematician will be
introduced and exercised while exploring advanced topics in graph theory and
making discoveries through independent research.
Prereq.: MATH 5835.

MATH 6955  Advanced Differential Equations  3 s.h.
Proofs of existence and uniqueness of nonautonomous, nonlinear equations.
Additional topics may include advanced linear systems, partial differential
equations, and integral equations.
Prereq.: MATH 5852 and either MATH 3705 or MATH 4855 or permission of
graduate coordinator.

MATH 6957  Partial Differential Equations  3 s.h.
An introduction to partial differential equations (PDE) and their applications.
The classification of the basic types of linear partial differential equations,
development of how boundary and initial conditions affect solutions,
exploration, and application of solution techniques for PDEs and explosions in
orthogonal functions will be presented.
Prereq.: MATH 3705 and MATH 3720 or equivalent.

MATH 6975  Complex Analysis  1  3 s.h.
Analytic and meromorphic functions of a complex variable, contour
integration, the Cauchy-Goursat theorem, Taylor and Laurent series, residues
and poles, conformal mapping. Credit will not be given for both MATH 4875
and MATH 6975.
Prereq.: MATH 3751 or permission of graduate coordinator.

MATH 6980  Topology  1  3 s.h.
Basic concepts of topological spaces and mappings between them, including
compactness, connectedness, and continuity. Credit will not be given for both
MATH 4880 and MATH 6980.
Prereq.: MATH 3721 Abstract Algebra I and MATH 3751 Real Analysis I, or
permission of graduate coordinator.

MATH 6981  Topology  2  3 s.h.
Separation, metrization, compactification. Additional topics will be selected
from point-set topology, fuzzy topology, algebraic topology, combinatorial
topology, topological algebra.
Prereq.: MATH 4880 or MATH 6980, or permission of graduate coordinator.

MATH 6990  Independent Study  1-3 s.h.
Study under the supervision of a staff member. May be repeated.
Prereq.: Consent of graduate coordinator.

MATH 6995  Special Topics  1-3 s.h.
Specialized topics selected by the staff. May be repeated up to 12 semester
hours.
Prereq.: Permission of graduate coordinator and department chair.

MATH 6995W  Special Topics Applied Time Series Analysis and
Forecasting  1-3 s.h.
Specialized topics selected by the staff. May be repeated up to 12 semester
hours.
Prereq.: Permission of graduate coordinator and department chair.

MATH 6996  Mathematical Project  1-3 s.h.
Individual research project culminating in a written report or paper, though not
as broad in scope as a thesis. May be repeated once if the second project is in
a different area of mathematics.

MATH 6999  Thesis  3 s.h.
A student may register for six semester hours in one semester or for three
semester hours in each of two semesters.

MATH 7005  Advanced Topics in Categorical Topology  3 s.h.
Content varies with each offering. Implements ideas from MATH 6915,
MATH 6980, MATH 6981, and studies categorical methods in topology
and related concrete categories. Emphasis on current literature and open
questions. May be repeated with approval of graduate coordinator.
Prereq.: MATH 6915, MATH 6980, MATH 6981, or equivalent, or permission of
the graduate coordinator.

MATH 7015  Advanced Topics in Foundations of Topology  3 s.h.
Content varies with each offering, implements ideas from MATH 6915,
MATH 6980, MATH 6981, and studies foundations of topology from a variety of
viewpoints (algebraic, categorical, logical, order theoretic, powerset theoretic,
set theoretic, etc.). Emphasis on current literature and open questions. May be
repeated with approval of graduate coordinator.
Prereq.: MATH 6915, MATH 6980, MATH 6981, or equivalent, or permission of
graduate coordinator.

MATH 7025  Advanced Topics in General Topology  3 s.h.
Content varies with each offering, implements ideas from MATH 6915,
MATH 6980, MATH 6981, and studies various topics in point-set topology.
Emphasis on current literature and open questions. May be repeated with
approval of graduate coordinator.
Prereq.: MATH 6980, MATH 6981, or equivalent, or permission of graduate
coordinator.

MATH 7035  Advanced Topics in Lattice-Valued Topology  3 s.h.
Content varies with each offering. Implements ideas from MATH 6915,
MATH 6980, MATH 6981, and studies topology from the standpoint of lattice-
valued (fuzzy) subsets. Emphasis on current literature and open questions.
May be repeated with approval of graduate coordinator.
Prereq.: MATH 6915, MATH 6980, MATH 6981, or equivalent, or permission of
the graduate coordinator.

MATH 7045  Advanced Topics in Topological Analysis  3 s.h.
Content varies with each offering. Implements ideas from MATH 6915,
MATH 6980, MATH 6981, and studies the overlap between topology and
abstract analysis (topological games, topological groups, separate versus joint
continuity, etc.). Emphasis on current literature and open questions. May be
repeated with approval of graduate coordinator.
Prereq.: MATH 6915, MATH 6980, MATH 6981, or equivalent, or permission of
the graduate coordinator.

MATH 7055  Seminar in Topology and Abstract Analysis  3 s.h.
Content varies with each offering. Implements ideas from MATH 6915,
MATH 6980, MATH 6981, and focuses on current research activities of
seminar participants. Student registrants are expected to make at least one
major presentation each month of the term. May be repeated with approval of
graduate coordinator.
Prereq.: Permission of graduate coordinator.